

OFFICE OF NAVAL RESEARCH

Contract NOOO14-96-C-0100

R&T Code 96PR03769

Technical Report No. 1

Side-Loop Polymers Based on the Hydrosilylation of Polybutadiene

by

Kurt Baum, Jean C. Baum
Fluorochem, Inc.,

and

Tai Ho
Naval Research Laboratory

Prepared for Publication

in the

Journal of the American Chemical Society

Fluorochem, Inc.
680 South Ayon Ave.
Azusa, California 91702

DTIC QUALITY INSPECTED 2

February 3, 1998

Reproduction in whole or in part is permitted for any purpose of the United States Government

This document has been approved for public release and sale;
its distribution is unlimited.

19980211 035

REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave Blank)		2. REPORT DATE 3 Feb 98		3. REPORT TYPE AND DATES COVERED
4. TITLE AND SUBTITLE Side-Loop Polymers Based on the Hydrosilylation of Polybutadiene			5. FUNDING NUMBERS N00014-96-C-01000 96 PR03769	
6. AUTHOR(S) Kurt Baum, Jean C. Baum and Tai Ho				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Flurochem, Inc. 680 S. Ayon Avenue, Azusa, CA 91702 and Naval Research Laboratory Washington DC, 20375-5342			8. PERFORMING ORGANIZATION REPORT NUMBER TR1	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) Office of Naval Research 800 North Quincy Street Arlington, VA 22217			10. SPONSORING/MONITORING AGENCY REPORT NUMBER	
11. SUPPLEMENTARY NOTES To be published in the Journal of the American Chemical Society				
12a. DISTRIBUTION/AVAILABILITY STATEMENT This document has been approved for public release and sale; its distribution is unlimited.			12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words) Hydrosilylation of hydride-terminated polydimethylsiloxane with polybutadiene in dilute solution yielded polysiloxane side-loops on a hydrocarbon base, a novel polymer architecture. When the ratio of silane to olefin was increased, the inherent viscosity of solutions dropped drastically, and polymer properties changed from tough rubbers to tacky materials. The results are rationalized on the basis of diminishing availability of olefin sites as the reaction proceeds. When one end of a difunctional silane attaches to an olefin site and no other olefin sites are available nearby, molecular motion eventually brings a remote olefin site in the molecule into proximity. Hydrosilylation then results in permanent ring folding. Subsequent hydrosilylations can then result in a dendrimer-like globular molecule. Contact angle measurements of side-loop adducts show temporal stability, indicating that the tendency of polydimethylsiloxane side chains to migrate to or away from the surface, depending on the medium, is circumvented by anchoring both ends.				
14. SUBJECT TERMS Polymer, silicones, hydrosilylation			15. NUMBER OF PAGES 15	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT	

Side-Loop Polymers Based on the Hydrosilylation of Polybutadiene

Kurt Baum* and Jean C. Baum

Fluorochem, Inc., 680 South Ayon Avenue, Azusa, California 91702

Tai Ho†

Naval Research Laboratory, Washington DC, 20375-5342

ABSTRACT: Hydrosilylation of hydride-terminated polydimethylsiloxane with polybutadiene in dilute solution yielded polysiloxane side-loops on a hydrocarbon base, a novel polymer architecture. When the ratio of silane to olefin was increased, the inherent viscosity of solutions dropped drastically, and polymer properties changed from tough rubbers to tacky materials. The results are rationalized on the basis of diminishing availability of olefin sites as the reaction proceeds. When one end of a difunctional silane attaches to an olefin site and no other olefin sites are available nearby, molecular motion eventually brings a remote olefin site in the molecule into proximity. Hydrosilylation then results in permanent ring folding. Subsequent hydrosilylations can then result in a dendrimer-like globular molecule. Contact angle measurements of side-loop adducts show temporal stability, indicating that the tendency of polydimethylsiloxane side chains to migrate to or away from the surface, depending on the medium, is circumvented by anchoring both ends.

† Present address: Department, of Chemistry, Virginia Polytechnic Institute and State University, Blacksburg, VA 24061

Introduction

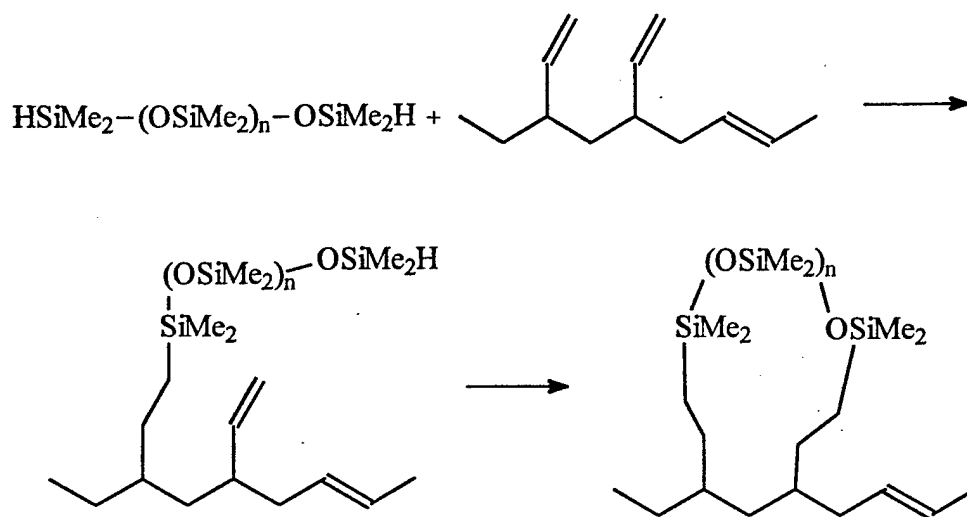
Silicones have become important commercial polymers because of a combination of properties, including high thermal stability,¹ low surface tension,^{1,2} low glass transition temperature,^{1,2} optical transparency^{1,2,3} and low dielectric constant.^{1,2} The materials, however, have relatively poor mechanical strength,^{1,4,5} generally requiring high filler loading to obtain acceptable properties. The poor strength is usually attributed to flaws or microcracks that grow readily because of the high mobility of the chains.^{5,6}

Recently, silicones have been found to be effective as anti-fouling marine coatings,⁷ providing potential replacements for toxic tin and copper based coatings currently in use. For this application, however, high filler loading is detrimental.

A potential alternative is to attach polysiloxanes as side chains to hydrocarbon polymers. Good fouling release coating properties have been attributed to low surface energy, low glass temperature, and temporal stability in water.⁸ When polysiloxane side chains were attached to polymethacrylate backbones, contact angle measurements indicated migration of the side chains to the polymer surface in air, but away from the surface on prolonged immersion in water.⁸ The result was unstable surface properties.

The approach taken here was to use a polymer architecture that could inhibit this type of chain migration. It was reasoned that if the polysiloxane chain could be attached to a main-chain polymer at both ends as a *side-loop*, the temporal instability would be minimized. Short chain monofunctional silanes, R_3SiH , have been hydrosilylated onto double bonds of polybutadiene and similar polyolefins.^{9,10,11}

Difunctional silanes, such as hydride-terminated polydimethylsiloxane (HPDMS) are available. Intermolecular reactions, however, would result in a highly cross-linked, unmanageable system, but intermolecular reactions should be avoided by high dilution. The formation of side-loops after the initial attachment of HPDMS is depicted in Scheme 1.



Scheme 1. Side-loop formation.

Polymer architectures are usually categorized as linear, branched and crosslinked.^{12,13,14} Recently, the exploration of novel polymer architectures has become one of the most active areas of polymer chemistry, and reviews have appeared covering dendrimers,^{15,16,17,18} polyrotaxanes,¹⁹ polycatenanes,¹⁹ and cyclic polymers.^{20,21} The concept of side loop polymers has been virtually unexplored. Thus, polymerization of divinyl monomers has yielded polymers with loops consisting of the original spacers

between vinyl groups.²² Also, when crosslinking of polystyrene by alkylation was carried out in dilute solution, only intramolecular crosslinking was obtained.²³

Experimental Section

Materials. THF and toluene (Aldrich HPLC grade) were used as received. Polybutadiene of M_n 100,000 (93% vinyl olefin) was used as received from Scientific Polymer Products, Inc. Hydride-terminated polydimethylsiloxane (M_n 400) was obtained from Hüls America Inc. Wilkinson's catalyst (tris(triphenylphosphine)-rhodium I) chloride and chloroplatinic acid were purchased from Aldrich.

Hydrosilylation of polybutadiene (general procedure). Polybutadiene was dissolved in toluene in a 1-liter flask equipped with a magnetic stirrer, a reflux condenser, a nitrogen inlet, and a heating mantle. Hydride-terminated polydimethylsiloxane and the catalyst tris(triphenylphosphine)-rhodium(I) chloride were added, and the mixture was refluxed under nitrogen until the IR spectra of aliquots indicated the absence of SiH absorption at 2163-2068 cm^{-1} (3-5 days). Details regarding quantities are given in Table I.

Slide coatings and moldings. Portions of the toluene solutions were concentrated with a rotary evaporator to give viscous solutions of 30-45% concentration. These solutions were used immediately, as gelatin resulted on prolonged storage. Microscope slides (1 x 3 inch) were coated with the material using a spin-coating technique.²⁴ Silanized slides were taped to the center post of a centrifuge with doubled tape, and the concentrated solution was added dropwise to the center of the spinning slide. The slides were then heated overnight in a 100 °C oven. Moldings

were prepared by pouring the concentrated solutions into a Teflon mold, and heating at 60-65°C for several days.

Inherent and intrinsic viscosities. Viscometric measurements were performed using a Cannon-Ubbelohde Semi-Micro type viscometer (No.50). The solvent was toluene, the temperature was maintained at 20 °C with a water bath. The inherent viscosity was measured at 0.5 or 0.1 g/dl, and the elapsed time was recorded with an optical viscosity timer (Model 821, Jupiter Instrument Company, Jupiter, Florida). The inherent viscosity of a polymer solution equals the intrinsic viscosity at infinite dilution.²⁵ For the materials investigated, the difference between the inherent viscosity measured at 0.5 g/dl and the intrinsic viscosity was estimated to be less than 5%.

Gel Permeation Chromatography. The equipment consisted of a Hewlett-Packard Series 1050 pump and two Altex spherogel AE columns (size 103 and 104, respectively) connected in series. The mobile phase was THF or toluene. Polymer contents in the effluent of the columns were detected with a Wyatt/Optilab 903 interferometric refractometer.

Contact angle. Contact angles were measured with a Cahn Dynamic Contact Angle Analyzer (model 312). Samples were prepared by dip-coating the material on glass slides (25 x 75 x 1 mm). Water purified with a Barnstead NANOpure water system was used as the probe liquid.

Results and Discussion

Polybutadiene was used as the polyolefin to test the concept of side-loop hydrosilylation. Hydrosilylations have been reported to take place much more rapidly at the vinyl double bonds of polybutadiene than at the internal double bonds.⁹ Therefore, polybutadiene with high vinyl content (93%) was used, with 100,000 molecular weight. Commercially available hydride-terminated polydimethylsiloxane of molecular weight 400 was used, and the hydrosilylation was catalyzed with Wilkinson's catalyst (tris(triphenylphosphine)-rhodium I chloride). The hydrosilylations were carried out in toluene solution, and were monitored by the disappearance of SiH absorption in the IR spectrum.

To avoid intermolecular hydrosilylations, it is desirable to keep the polymer concentration at a level that expanded molecules do not extensively overlap with each other. Correlations between the unperturbed dimension, r_0 , in cyclohexane and the molecular weight for polybutadienes of different compositions have been reported.²⁶ According to those correlations, specific volume in cyclohexane at 25 °C for polybutadiene of molecular weight 220,000, containing 25% terminal vinyl groups is 162 cm³/g. This number was used to estimate the initial concentrations of the reactants. In actuality the reactions were carried out in toluene, and polybutadiene containing 93% terminal vinyl group was used. Although the effects of solvent are expected to be small, as solubility parameter for cyclohexane, 8.2 (cal/cm³)=BD, is quite close to the solubility parameter of toluene, 8.9 (cal/cm³)=BD. For a given molecular weight, the specific volume for polybutadiene increases with increase in

terminal vinyl content.²⁶ The concentrations used in this study were substantially below the theoretical maximum for total mutual exclusion as derived above.

For ease in comparing the effect of the extent of hydrosilylation of the double bonds of polybutadiene on polymer properties, fixed equivalent ratios of hydride to vinyl double bonds were used. The hydrosilylation reactions are summarized in Table I; the adducts are designated by the relative equivalents of hydride and vinyl bonds (H1V3 designates a 1:3 ratio). The nominal molecular weights were calculated on the basis of reaction stoichiometry, and are high enough to suggest that good polymer properties could be expected even without crosslinking.

Table I
Hydrosilylation of Polybutadiene^a

adduct	wt silane	eq silane ^b	wt pbd	eq vinyl ^c	% PDMS	nominal MW ^d
H1V3	8.01	0.0400	6.99	0.1202	53	215,000
H1V2	9.48	0.0474	5.52	0.0949	63	272,000
H1V1	11.62	0.0581	3.38	0.0581	77	444,000
H2V1	13.1	0.0655	1.91	0.0328		

^a 750 mL toluene as solvent, 50 mg Wilkinson's catalyst. ^b Eq wt 200. ^c 93% vinyl content. ^d Based on stoichiometry.

Molded objects were prepared from H1V3, H1V2 and H1V1 by removing solvent under vacuum to give viscous solutions and then drying the solutions in a PTFE mold. The H1V3 samples were tough, strong elastomers, whereas the H1V2 samples were weak and the H1V1 were tacky. The concentrated solutions could not be stored for long periods, and began to gel in several hours. The dried samples did not redissolve completely in toluene. Although IR indicated complete consumption of

hydride, it appears that small amounts remained in hindered positions and the accelerated intermolecular reaction on solvent removal resulted in crosslinking. Even extending the hydrosilylation after the normal period with the addition of 3,3-dimethylbutene did not prevent the gelling. Similar results were obtained when the reaction mixture was transferred to an autoclave and treated with ethylene under the same conditions.

The degradation of elastomer properties after sufficient silane is added to consume more than half of the double bonds was unexpected. Depolymerization of the base polymer under the polymerization conditions could be considered. However, Crivello²⁷ recently showed that, although polybutadiene with 9% vinyl content degrades in the presence of Wilkinson's catalyst in toluene, no such drop in molecular weight is observed with 93% vinyl polybutadiene.

Viscometric Studies. To gain more insight into the reaction, solution viscosities were examined. The results are shown in Table II. The observed order of the inherent viscosities is opposite the order of the molecular weights expected on the basis of stoichiometry. The most notable viscosity decrease comes after the reaction midpoint (H1V2).

Table II
Inherent Viscosity of Adducts

adduct	concentration (g/dl)	inherent viscosity (dl/g)
H1V3	0.5	0.56
H1V2	0.5	0.32
H1V1	0.5	0.10
H2V1	0.5	0.05

Intrinsic viscosity is related to the molecular weight by the Mark-Houwink equation:

$$\text{intrinsic viscosity} = k (\text{MW})^a \quad (1)$$

For polybutadiene containing 65% terminal vinyl groups in toluene at 25 °C, the k value is 1.10×10^{-3} dl/g and a is 0.62, the corresponding values for polydimethylsiloxane are 0.22×10^{-3} dl/g and 0.65, respectively.²⁸ Since for polybutadienes of different vinyl contents, the k value decreases while the a value increases with increase in terminal vinyl content, the above parameters should apply to the polybutadiene used in these reactions, i.e. 93% 1,2-vinyl, reasonably well. The intrinsic viscosity for the polybutadiene used was 1.23 dl/g, and the inherent viscosity of the hydride-terminated polydimethylsiloxane at 0.1 g/dl was 9.50×10^{-3} dl/g. Both values are in agreement with predictions by the Mark-Houwink equation using parameters cited above. The Mark-Houwink parameters also indicate that toluene is a much better solvent for polybutadiene than polydimethylsiloxane. Thus, the reversed inherent viscosity-molecular weight relation observed in the polymers may be due partially to the difference in solubility for polybutadiene and polydimethylsiloxane. Polymers prepared with excess hydrides, although of higher molecular weight, are less expansive, as the polydimethylsiloxane contents in these polymers are higher, and polydimethylsiloxane is less soluble in toluene than polybutadiene. Nevertheless, the silane contents of the polymers, as shown in Table I, are all greater than 53%, and it does not seem likely that this change in solubility properties could result in an order of magnitude reduction in viscosity.

Solubility and refractive index differences between polybutadiene and silicone prevented molecular weight determinations of the adducts by GPC. However, unreacted hydride terminated PDMS (MW 400) could be determined with toluene as the mobile phase. The proportionality obtained from GPC traces for solutions containing the PDMS at known concentration was used to correct the viscosity data. The inherent viscosities for the macromolecular products after the correction were 0.06, 0.11, 0.33, and 0.58 dl/g for runs H2V1, H1V1, H1V2, and H1V3, compared with 0.05, 0.10, 0.32, and 0.56 dl/g before the correction. Thus, the effect of free PDMS on the viscometric measurements was minimal.

Another possible cause of discrepancies in the viscosity data is crosslinking of the adducts on storage before viscosities are measured. This possibility was tested by repeating the hydrosilylation experiments at half the concentration of the previous experiments. The inherent viscosities were 0.28, 0.17, 0.09, and 0.08, dl/g for runs H1V3, H1V2, H1V1, and H2V1, respectively. The values were approximately halved for H1V3 and H1V2, and changes were insignificant for H1V1, and H2V1, which theoretically have no free olefin. Thus, there still is a large unexplained reduction in viscosity as the molecular weight increases as the hydrosilylation proceeds.

A rationalization of the changes in solution viscosity, as well as the characteristics of isolated polymers is based on the changing availability of vinyl groups as the reaction proceeds. The initial hydrosilylation step is slow because the hydride, olefin and catalyst must unite in dilute solution. After one end of a PDMS molecule is attached, the local concentration of vinyl groups for the remaining end increases enormously, and ring closure takes place rapidly at an adjacent or nearby olefin site.

As the reaction proceeds, chain sites with two nearby free vinyl groups ultimately become exhausted, and when a PDMS molecule attaches to an olefin, no additional local sites are available for loop formation. Eventually, motion of the chain brings a distant vinyl group in the polyolefin molecule into proximity for hydrosilylation, and permanent ring folding is the result. Repetitions of the process may "stitch" the molecule into a spherical shape. Thus, as the reaction proceeds, reduced chain entanglement results in lower viscosity in solution, and reduced strength of isolated films.

There is considerable current interest in dendrimers and hyperbranched polymers.^{15,16,17,18} Hyperbranched polymers are obtained by simple polymerization methods and have some shape similarities with dendrimers. There is little control, however, over uniformity of molecular weight or shape of hyperbranched polymers. Even dendrimers constructed layer by layer have irregularities that become more distorted with each generation. The present method offers an alternative approach to globular macromolecules. The spherical molecule is stitched together from a long polyolefin rather than being built up in layers. Molecular weight uniformity is limited mainly by the uniformity of available polyolefins. Unused olefin sites can potentially be used to introduce other functional groups on the surface. Notably, an extremely simple one-step synthesis method is used, based on commercially available starting materials.

Contact Angle Analysis. Contact angles of water on these materials appear to be independent of the composition. The advancing contact angle of water on the

products from run H2V1 was 94° , and the receding contact angle was 80° , the corresponding values were 91 and 79° for run H1V1, 91 and 83° for run H1V2, and 92 and 75° for run H1V3. Interestingly, these properties are temporally stable. For example, the water contact angles on products from run H1V3 that had been immersed in water continuously for six days were 88° , advancing, and 75° , receding. In comparison, water contact angles on freshly prepared polybutadiene film were 108° , advancing, and 86° , receding; the same properties after eight days' immersion in water were 92 and 20° , respectively. Thus, the tendency of polydimethylsiloxane side chains to migrate into the polymer or to the surface, depending on the medium,⁸ is circumvented by anchoring both ends.

Conclusions. As the hydride to vinyl ratio is increased in the dilute hydrosilylation of hydride-terminated polydimethylsiloxane with polybutadiene, the inherent viscosity of the solution decreases dramatically, and polymer properties change from tough rubbers to tacky materials. For low hydride to vinyl ratio, the results are explained on the basis of the formation of side-loops when attachment takes place between nearby vinyl groups. At higher ratios, hydrosilylation at an isolated olefin site may give a hydride-terminated side-chain with no nearby vinyl groups. When molecular motion brings a remote olefin site in the molecule into proximity, hydrosilylation results in permanent ring folding. Subsequent hydrosilylations can then result in a compact, dendrimer-like molecule. Contact angle measurements of side-loop adducts show temporal stability, indicating that the tendency of polydimethylsiloxane side chains to migrate to or away from the surface, depending on

the medium, is circumvented by anchoring both ends. The concept of side-loop polymers and the new approach to dendrimers potentially have broader applicability to other systems.

Acknowledgment. This work was supported by the Office of Naval Research.

References

-
- ¹ Noll, W., "Chemistry and Technology of Silicones", Academic Press, New York, NY, 1968, 388.
 - ² Voronkov, M. G.; Milenshkevich, V. P.; Yuzhelevskii, Yu. A. "The Siloxane Bond", Consultants Bureau, New York, NY, 1978.
 - ³ Lewis, F. M. in "High Polymers", Vol. XXIII Pt.2, Kennedy, J. P. and Tornquist, E. G. M., eds, Ch. 8, Interscience, New York, NY, 1969.
 - ⁴ Polmanteer, K. E. *J. Elastoplastics*, 1970, 2, 165.
 - ⁵ Yilgor, I.; McGrath, J. E., *Adv. Polym. Sci.* 1988, 86, 1-86.
 - ⁶ Smith, T. L., *Rubber Chem. Technol.* 1978, 51, 225.
 - ⁷ Ho, T.; Wynne, K. J., *Am. Chem. Soc. Polym. Prepr.*, 1996, 37 (2), 741-2, and references cited therein.
 - ⁸ Merra, A. E.; Pike, J. K.; Wynne, K. J., *Am. Chem. Soc. Polym. Prepr.*, 1996, 37 (2), 765-6.
 - ⁹ Guo, X.; Farwaha, R.; Rempel, G. L., *Macromolecules*, 1990, 23 (24), 5047-5054.
 - ¹⁰ Gabor, A. H.; Lehner, E. A.; Mao, A.; Schneggenburger, L. A.; Ober, C. K. *Am. Chem. Soc. Polym. Prepr.*, 1992, 33 (2), 136-7.

-
- ¹¹ Jin, H.; Liu, Z.; Xu, J., *Mo Kexue Yu Jishu*, 1992, 12 (4), 35-40 (*Chem. Abstr.*, 120, 324730).
- ¹² G. Odian, "Principles of Polymerization," McGraw-Hill Book Co., New York, N. Y., 1970, p. 16-19.
- ¹³ Saunders, K. J., "Organic Polymer Chemistry," Chapman and Hall, New York, N. Y., 1988, p. 27-36.
- ¹⁴ Allcock, H. R.; Lampe, F. W., "Contemporary Polymer Chemistry," Prentice Hall, Englewood Cliffs, N. J., 1990, p. 3-8.
- ¹⁵ Voit, B. I., *Acta Polymer*, 1995, 46, 87-99.
- ¹⁶ Tomalia, D. A.; Esfand, R., *Chem. Ind. (London)* 1997, (11), 416-420.
- ¹⁷ Frechet, M. J.; Hawker, C. J.; Wooley, K. L., *J. Macromol. Sci.- Pure Appl. Chem.*, 1994, A31(11), 1624-1645.
- ¹⁸ Percec, V.; Chu, P.; Ungar, G.; Zhou, J., *J. Am. Chem. Soc.*, 1995, 117, 11441-11454.
- ¹⁹ Gibson, H. W.; Bheda, M. C.; Engen, P. T., *Prog. Polym. Sci.* 1994, 19, 843-945.
- ²⁰ Maravigna, P.; Montaudo, G. in "Comprehensive Polymer Science". Eds. Allen; G. A.; Bevington, J. C., Pergamon, Oxford, 1989, Vol. 5, Chapter 5.
- ²¹ "Cyclic Polymers", ed. Semlyen, J. A., Elsevier Applied Science, London, 1986.
- ²² Butler, G. B.; Corfield, G. S.; Aso, C. *Prog. Polym. Sci.* 1975, 71, 71. Butler, G. B., *J. Polym. Sci., Polym. Symp.* 1978, 64, 71-93.
- ²³ Davankov, V. A.; Tsyurupa, M. P. *Angew. Makromol. Chem.* 1980, 91, 127.
- ²⁴ Baty, A. M.; Suci, P. A.; Tyler, B. J.; Geesey, G. G. *J. Colloid Interface Sci.* 1996, 177(2), 307-315.

²⁵ Billmeyer, F.W. Textbook of Polymer Science; John Wiley and Sons, Inc. New York; 1971, Chap.3.

²⁶ Bandrup, J; Immergut, E.H. Polymer Handbook, John Wiley and Sons, Inc. New York; 1989, p. VII/33.

²⁷ Malik, R.; Crivello, J. V., *J. Macromol. Sci., Pt. A: Pure and Appl. Chem.*, 1997, A34 (2), 247-263.

²⁸ Bandrup, J; Immergut, E.H. Polymer Handbook, John Wiley and Sons, Inc., New York; 1989, Sec. VII.